

$$b.) \text{ Fläche } \underline{I} = A_1 + A_2 + A_3 + A_6$$

$$f(x) = -x^2 + 2 = 0 \Rightarrow x_{1,2} = \pm\sqrt{2}$$

$$\begin{aligned} \text{Fläche } \underline{I} &= \int_{-\sqrt{2}}^{\sqrt{2}} (-x^2 + 2) dx = \left[ -\frac{x^3}{3} + 2x \right]_{-\sqrt{2}}^{\sqrt{2}} = -\frac{2\sqrt{2}}{3} + 2\sqrt{2} \\ &\quad - \left\{ +\frac{2\sqrt{2}}{3} - 2\sqrt{2} \right\} = 4\sqrt{2} - \frac{4}{3}\sqrt{2} = \frac{8}{3}\sqrt{2} \approx \underline{\underline{3,771}} \end{aligned}$$


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$$\text{Fläche } \underline{II} = A_2 + A_3 + A_4 + A_5$$

$$\text{Schnitt } f \text{ mit } g \Rightarrow -x^2 + 2 = 2x^2 - 1 \Rightarrow 1 = x^2 \Rightarrow x_{1,2} = \pm 1$$

$$\begin{aligned} \text{Fläche } \underline{II} &= \int_{-1}^{+1} f(x) - g(x) dx = \int_{-1}^{+1} ((-x^2 + 2) - (2x^2 - 1)) dx \\ &= \int_{-1}^{+1} (-3x^2 + 3) dx = \left[ -3 \cdot \frac{x^3}{3} + 3x \right]_{-1}^{+1} = -1 + 3 - \{-1 - 3\} \\ &= 4 \end{aligned}$$


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$$\begin{aligned} \text{Fläche } \underline{III} = A_3 + A_6 &= \int_0^{\sqrt{2}} (-x^2 + 2) dx = \left[ -\frac{x^3}{3} + 2x \right]_0^{\sqrt{2}} \\ &= -\frac{2\sqrt{2}}{3} + 2\sqrt{2} = \frac{4}{3}\sqrt{2} \approx \underline{\underline{1,886}} \end{aligned}$$


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$$\begin{aligned} \text{Fläche } \underline{IV} = A_7 &= \int_{-2}^{-\sqrt{2}} |-x^2 + 2| dx = \int_{-2}^{-\sqrt{2}} (x^2 - 2) dx = \left[ \frac{x^3}{3} - 2x \right]_{-2}^{-\sqrt{2}} \\ &= \frac{-2\sqrt{2}}{3} + 2\sqrt{2} - \left\{ -\frac{8}{3} + 4 \right\} = \frac{4}{3}\sqrt{2} + \frac{8}{3} - 4 \approx \underline{\underline{0,552}} \end{aligned}$$