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$$A(z) = \int_1^z \frac{1}{(x+1)^2} dx = \left[-\frac{1}{(x+1)^1} \right]_1^z = -\frac{1}{z+1} - \left\{ -\frac{1}{1+1} \right\}$$

$$A(z) = -\frac{1}{z+1} + \frac{1}{2} \Rightarrow \lim_{z \rightarrow \infty} A(z) = \frac{1}{2}$$

Fig. 3

$$A(z) = \int_2^z e^{-\frac{1}{2}x} dx = \left[e^{-\frac{1}{2}x} \cdot \frac{1}{-\frac{1}{2}} \right]_2^z = \left[-2 \cdot e^{-\frac{1}{2}x} \right]_2^z =$$
$$= -2 \cdot e^{-\frac{1}{2}z} - \left\{ -2 \cdot e^{-\frac{1}{2} \cdot 2} \right\} = \underbrace{-2 \cdot e^{-\frac{1}{2}z}}_{\rightarrow 0 \text{ für } z \rightarrow \infty} + 2 \cdot e^{-1}$$

$$\lim_{z \rightarrow +\infty} A(z) = \frac{2}{e}$$

Fig. 4

$$A(z) = \int_z^1 \frac{2}{x^3} dx = \left[\frac{2}{x^2} \cdot \frac{1}{-2} \right]_z^1 = \left[-\frac{1}{x^2} \right]_z^1 = -\frac{1}{1} - \left\{ -\frac{1}{z^2} \right\}$$

$$A(z) = \frac{1}{z^2} - 1 \text{ für } z \rightarrow 0 \text{ strebt } \underline{A(z) \rightarrow +\infty}$$

Fig. 5

$$A(z) = \int_z^4 \frac{4}{\sqrt{x}} dx = \left[4 \cdot \sqrt{x} \cdot \frac{1}{\frac{1}{2}} \right]_z^4 = \left[8 \cdot \sqrt{x} \right]_z^4 = 8 \cdot \sqrt{4} - \left\{ 8 \cdot \sqrt{z} \right\}$$

$$A(z) = 16 - 8\sqrt{z} \Rightarrow \lim_{z \rightarrow 0} A(z) = 16$$
