

Nr. 14) $u(x) = 2x - 1$; $v(x) = -x + 2$; $w(x) = 3x - 2$

a) $u(v(x)) = 2 \cdot (-x + 2) - 1 = -2x + 4 - 1 = \underline{\underline{-2x + 3}}$

$$v(u(x)) = -(2x - 1) + 2 = -2x + 1 + 2 = \underline{\underline{-2x + 3}}$$

$$u(w(x)) = 2 \cdot (3x - 2) - 1 = 6x - 4 - 1 = \underline{\underline{6x - 5}}$$

$$w(u(x)) = 3 \cdot (2x - 1) - 2 = 6x - 3 - 2 = \underline{\underline{6x - 5}}$$

b) $\underbrace{m_1 x + c_1}_{u(x)}$; $\underbrace{m_2 x + c_2}_{v(x)}$

$$u(v(x)) = m_1 \cdot (m_2 x + c_2) + c_1 = \underbrace{m_1 m_2 x + m_1 c_2 + c_1}_{= \underline{\underline{m_3 x + c_3}}}$$

$\Rightarrow u(v(x))$ ist eine lineare Funktion

c) $(f \circ g)(x) = (g \circ f)(x)$; $f(x) = 9x + 2$; $g(x) = 3x + a$

$$g(3x + a) + 2 = 3 \cdot (9x + 2) + a$$

$$\cancel{27x} + 9a + 2 = \cancel{27x} + 6 + a \quad | -a - 2$$

$$8a = 4$$

$$\underline{\underline{a = \frac{1}{2}}}$$

Für $a = \frac{1}{2}$ gilt $f \circ g = g \circ f$

d) $u(x) = m_1 \cdot x + c_1$; $v(x) = m_2 x + c_2$

$$u(v(x)) = v(u(x))$$

$$m_1(m_2 x + c_2) + c_1 = m_2(m_1 x + c_1) + c_2$$

$$\cancel{m_1 m_2 x} + m_1 c_2 + c_1 = \cancel{m_2 m_1 x} + m_2 c_1 + c_2 \quad | -c_2 - c_1$$

$$m_1 c_2 - c_2 = m_2 (c_1 - c_1)$$

$$c_2 (m_1 - 1) = c_1 (m_2 - 1) \quad | \cdot \frac{1}{(m_2 - 1) \cdot c_2}$$

Für $\underline{\underline{\frac{m_1 - 1}{m_2 - 1} = \frac{c_1}{c_2}}}$ ist $\underline{\underline{u \circ v = v \circ u}}$