

Nr. 2) $A(3|0|0)$ $B(3|5|0)$ $H(0|0|4)$

$$E_1: \underline{\underline{\vec{x}}} = \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix} + r \begin{pmatrix} 3-3 \\ 5-0 \\ 0-0 \end{pmatrix} + s \begin{pmatrix} 0-3 \\ 0-0 \\ 4-0 \end{pmatrix} = \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix} + r \begin{pmatrix} 0 \\ 5 \\ 0 \end{pmatrix} + s \begin{pmatrix} -3 \\ 0 \\ 4 \end{pmatrix}$$

$$E_2: \underline{\underline{\vec{x}}} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + r \begin{pmatrix} 3 \\ 5 \\ 0 \end{pmatrix} + s \begin{pmatrix} 0 \\ 5 \\ 4 \end{pmatrix} = r \begin{pmatrix} 3 \\ 5 \\ 0 \end{pmatrix} + s \begin{pmatrix} 0 \\ 5 \\ 4 \end{pmatrix}$$

Nr. 3)

a) $\begin{pmatrix} 8 \\ 0 \\ 6 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} + r \begin{pmatrix} 2 \\ 1 \\ 3 \end{pmatrix} + s \begin{pmatrix} 3 \\ -2 \\ 1 \end{pmatrix}$

$$\begin{array}{l|l|l} 2r + 3s = 7 & \cdot 1 & \cdot 3 \\ r - 2s = 0 & \cdot (-2) & \\ \hline 3r + s = 7 & & \cdot (-2) \end{array}$$

$$2r + 3s = 7 \Rightarrow 2r = 7 - 3 \cdot 1 = 4 \Rightarrow r = 2$$

$$\left. \begin{array}{l} 7s = 7 \Rightarrow s = 1 \\ 7s = 7 \Rightarrow s = 1 \end{array} \right\} \Rightarrow \underline{\underline{P(8|0|6) \in E}}$$

b) $\begin{pmatrix} 2 \\ 1 \\ 3 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} + r \begin{pmatrix} 2 \\ 1 \\ 3 \end{pmatrix} + s \begin{pmatrix} 3 \\ -2 \\ 1 \end{pmatrix}$

$$\begin{array}{l|l|l} 2r + 3s = 1 & \cdot 1 & \cdot 3 \\ r - 2s = 1 & \cdot (-2) & \\ \hline 3r + s = 4 & & \cdot (-2) \end{array}$$

$$2r + 3s = 1$$

$$\left. \begin{array}{l} 7s = -1 \Rightarrow s = -\frac{1}{7} \\ 7s = -5 \Rightarrow s = -\frac{5}{7} \end{array} \right\} \Rightarrow \underline{\underline{P(2|1|3) \notin E}}$$

c) $P(16|-3|11) \in E$

d) $P(6|-1|5) \notin E$