

Nr. 5) a)
$$E: \underline{\underline{\left[\vec{x} - \begin{pmatrix} -2 \\ 7 \\ -1 \end{pmatrix} \right] \cdot \begin{pmatrix} +3 \\ -3 \\ +5 \end{pmatrix} = 0}}$$

b)
$$E: \underline{\underline{\left[\vec{x} - \begin{pmatrix} 11 \\ 21 \\ 23 \end{pmatrix} \right] \cdot \begin{pmatrix} 6 \\ 1 \\ 0 \end{pmatrix} = 0}}$$

c)
$$\vec{OA} = \vec{n} = \begin{pmatrix} 2-0 \\ -1-0 \\ 2-0 \end{pmatrix} = \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix}$$

$$E: \underline{\underline{\left[\vec{x} - \begin{pmatrix} 4 \\ -2 \\ 4 \end{pmatrix} \right] \cdot \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix} = 0}}$$

d) E in Parameterform

$$E: \vec{x} = \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix} + r \begin{pmatrix} 2 \\ -2 \\ -2 \end{pmatrix} + s \begin{pmatrix} 3 - (-1) \\ 0 - 1 \\ -3 - 1 \end{pmatrix} = \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix} + r \begin{pmatrix} 2 \\ -2 \\ -2 \end{pmatrix} + s \begin{pmatrix} 4 \\ -1 \\ -4 \end{pmatrix}$$

$$\vec{n}^* = \begin{pmatrix} 2 \\ -2 \\ -2 \end{pmatrix} \times \begin{pmatrix} 4 \\ -1 \\ -4 \end{pmatrix} = \begin{pmatrix} 8 - (+2) \\ -8 - (-8) \\ -2 - (-8) \end{pmatrix}$$

$$\begin{array}{r} 2 \quad 4 \\ -2 \quad -1 \\ -2 \quad -4 \\ 2 \quad 4 \\ -2 \quad -1 \\ -2 \quad -4 \end{array}$$

$$\vec{n}^* = \begin{pmatrix} 6 \\ 0 \\ 6 \end{pmatrix} \Rightarrow \vec{n} = \frac{1}{6} \begin{pmatrix} 6 \\ 0 \\ 6 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$$

$$E: \underline{\underline{\left[\vec{x} - \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix} \right] \cdot \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = 0}}$$